

# Baryon form factors at BESIII

WANG Yadi (for BESIII Collaboration)

(Helmholtz-Institut Mainz (GSI), Mainz 55128, Germany)

**Abstract:** With the data collected by the BESIII detector at the BEPCII  $e^+e^-$  collider in 2011~2013, the cross section of  $e^+e^- \rightarrow p\bar{p}$  at 12 center-of-mass energies from 2.2324 to 3.6710 GeV was measured. The prospect of new results with the larger  $e^+e^-$  scanning data, collected in 2014 and 2015, is reported. The measurement of  $p\bar{p}$  form factor with ISR has also been studied using both tagged and untagged methods. With the good performances of BESIII, the feasibility of  $n\bar{n}$  form factor measurement in both ISR mode and scan mode is also reported. The preliminary but unexpected result of form factors of  $\Lambda\bar{\Lambda}$  measurement is shown, as well as the expectation from the data collected at the threshold of  $e^+e^- \rightarrow \Lambda_c\bar{\Lambda}_c$ . Also expected from these data is a measurement of form factors of all the other hyperons by BESIII.

**Key words:** Form factors; Baryons; Hyperons; BESIII

**CLC number:** O572.3      **Document code:** A      doi:10.3969/j.issn.0253-2778.2016.04.012

**Citation:** WANG Yadi. Baryon form factors at BESIII[J]. Journal of University of Science and Technology of China, 2016,46(4):337-342.

## BESIII 上的重子形状因子

王雅迪(BESIII 合作组)

(美因茨亥姆霍兹研究所,美因茨 55128,德国)

**摘要:** 利用在 2011~2013 年 BEPCII 对撞机上的 BESIII 探测器收集的数据,测量了  $e^+e^- \rightarrow p\bar{p}$  在 2.2324~3.6710 GeV 之间 12 个质心系能量点的截面。期待利用在 2014 年和 2015 年收集的更大的  $e^+e^-$  扫描数据样本做更进一步测量。通过标记和不标记初态辐射光子的方法,对  $p\bar{p}$  形状因子进行了测量。利用 BESIII 的优良探测器表现,利用标记和不标记初态辐射光子的方法,对  $n\bar{n}$  形状因子的测量进行了可行性研究。同时也一并报道了  $\Lambda\bar{\Lambda}$  的形状因子的初步但不符合理论预期的结果,及利用在  $e^+e^- \rightarrow \Lambda_c\bar{\Lambda}_c$  阈值上收集的数据的预期。也期望 BESIII 能对其他超子的形状因子进行测量。

**关键词:** 形状因子;重子;超子;BESIII

## 0 Introduction

The measurements of baryon form factors

(FFs) in space-like region as well as in the time-like region provide fundamental information on baryon structure, giving crucial tests also to

**Received:** 2015-11-30; **Revised:** 2016-04-20

**Foundation item:** Supported by German Research Foundation DFG under Collaborative Research Center (CRC-1044).

**Biography:** WANG Yadi, female, born in 1984, PhD. Research field: high energy physics. E-mail: wangyd@ihep.ac.cn

models of hadron internal structure in general. Looking back on the history, the experimental results on FFs have driven and renewed models which are trying to explain FFs of Nucleons at low and high  $q^2$ , in the space-like region as well as in the time-like region. In a parity, time reversal and gauge invariant theory, the structure of any non-point-like particle of spin  $S$  is parametrized in terms of  $(2S + 1)$  FFs. Hence baryons with  $\frac{1}{2}$  spin, which are considered here, are described by two electromagnetic FFs.

In the time-like (TL) region, assuming a metric where the momentum transfer squared  $q^2$  is positive, the FFs have complex values, and their module can be measured by means of cross section and angular distribution measurement. By looking into the polarization of the outgoing baryons, the information on the relative phase can be achieved. The Sachs FFs, electric  $G_E$  and magnetic  $G_M$ , are introduced as linear combinations of the Dirac and Pauli FFs<sup>[1]</sup>. The Born cross section, that is the one virtual photon channel, is supposed to be the dominant one in the time-like region. That means the final states have the photon quantum numbers, in particular, the same, negative, charge conjugation. As a consequence there should be a forward/backward symmetry. The two virtual photons would have the opposite one and the interference between these two contributions should produce a forward/backward asymmetry. Indeed a small asymmetry has been found in  $e^+e^- \rightarrow \gamma_{\text{ISR}} p \bar{p}$ <sup>[9-10]</sup>. Conversely, in the space-like region at high  $q^2$  the very different behaviour of  $G_E$  and  $G_M$  has been assumed to be due to a strong contribution from the two-photon exchange. The Born cross section can be written as a function of  $G_E$  and  $G_M$ , as in Eq. (1). The differential Born cross section can be written as in Eq. (2), by which the FFs ( $|G_E|$  and  $|G_M|$  or  $R = \left| \frac{G_E}{G_M} \right|$ ) can be measured.

$$\sigma_{\text{Born}} = \frac{4\pi\alpha^2\beta\mathcal{C}}{3q^2} \left[ |G_M|^2 + \frac{1}{2\tau} |G_E|^2 \right] \quad (1)$$

$$\frac{d\sigma_{\text{Born}}}{d\Omega} = \frac{\alpha^2\beta\mathcal{C}}{4q^2} \left[ (1 + \cos^2\theta) |G_M|^2 + \frac{1}{\tau} \sin^2\theta |G_E|^2 \right] \quad (2)$$

The factor  $\mathcal{C}$  is a correction to the Born cross section, due to Coulomb interaction between the outgoing charged baryons. Until now  $\mathcal{C}$  has been supposed to be the same as for point-like fermions, because of the long range Coulomb interaction. Analyticity of the Dirac and Pauli FF requires  $G_E(4M^2) = G_M(4M^2)$ . However it might be that some of these assumptions (that have never been under discussion) have to be reviewed, as it seems according to the present data on baryon FFs. For this reason it is worthwhile to collect more data on this topic. BESIII is a detector on a  $e^+e^-$  collider with very good performances that provides a good environment for measuring the FFs of baryons.

## 1 Proton FFs

In the TL region, measurements of proton FFs have been performed by means of  $e^+e^- \rightarrow p\bar{p}$ <sup>[2-7]</sup>, the radiative return  $e^+e^- \rightarrow \gamma_{\text{ISR}} p\bar{p}$ <sup>[8-10]</sup>, and also  $p\bar{p} \rightarrow e^+e^-$ <sup>[11-14]</sup>. While there are many, somewhat consistent, measurements concerning the total cross section, there are few, not consistent, data on the ratio  $R = \left| \frac{G_E}{G_M} \right|$ , mostly from BABAR<sup>[9]</sup> and PS170<sup>[11]</sup>.

Recently, based on 157 pb<sup>-1</sup> collected at 12 scan points between 2.22 and 3.71 GeV in 2011 and 2012, proton FFs have been measured at BESIII<sup>[15]</sup>. The product of proton and anti-proton selection efficiency times initial-state-radiation (ISR) up to the next-to-leading (NLO) correction factor,  $\epsilon(1 + \delta)$ , estimated by means of ConExc<sup>[16]</sup>, is about 66% at 2.23 GeV, with a 15% reduction at 4 GeV. After ISR correction, cross section and effective FF are extracted according to Eq. (3) and Eq. (4). The cross section is shown in Fig. 1(a). In Fig. 1(b)  $R$ , as extracted from the angular distribution of the proton, is shown, too. The method of moments (MM) (Eq. (5)) has also been used to evaluate  $R$ ,

see Tab. 1. The cross section has been measured with an accuracy between 6.0% and 18.9% up to  $\sqrt{s} < 3.08$  GeV, improving the previous results.  $G_M$  has also been measured.

$$\sigma_{\text{Born}} = \frac{N_{\text{obs}} - N_{\text{bkg}}}{\mathcal{L}_{\epsilon}(1 + \delta)} \quad (3)$$

$$|G| = \sqrt{\sigma_{\text{Born}}} \left(1 + \frac{1}{2\tau}\right) \left(\frac{4\pi\alpha^2\beta\ell}{2E_{\text{CM}}^2}\right) \quad (4)$$

$$\langle \cos^2\theta_p \rangle = \frac{1}{N_{\text{norm}}} \int \frac{2\pi\alpha^2\beta\mathcal{C}}{4s} \cos^2\theta_p \cdot \left[ (1 + \cos^2\theta_p) |G_M|^2 + \frac{4m_p^2}{s}(1 - \cos^2\theta_p) |R|^2 |G_M|^2 \right] d\cos\theta_p \quad (5)$$

**Tab. 1 Results on  $R$  and  $G_M$  by fitting the proton angular distribution as well as by the method of moments at different c. m. energies**

$\sqrt{s}/\text{MeV}$	$ G_E/G_M $	$ G_M (\times 10^{-2})$
Fit on $\cos\theta_p$		
2232.4	$0.87 \pm 0.24 \pm 0.05$	$18.42 \pm 5.09 \pm 0.98$
2400.0	$0.91 \pm 0.38 \pm 0.12$	$11.30 \pm 4.73 \pm 1.53$
3050.0~3080.0	$0.95 \pm 0.45 \pm 0.21$	$3.61 \pm 1.71 \pm 0.82$
Method of moments		
2232.4	$0.83 \pm 0.24$	$18.60 \pm 5.38$
2400.0	$0.85 \pm 0.37$	$11.52 \pm 5.01$
3050.0~3080.0	$0.88 \pm 0.46$	$3.34 \pm 1.72$

At present, the precision of  $R$  is still dominated by statistics. In 2014 and 2015, BESIII has collected more data by means of an energy scan. These data will provide the opportunity to get better results on proton FFs.

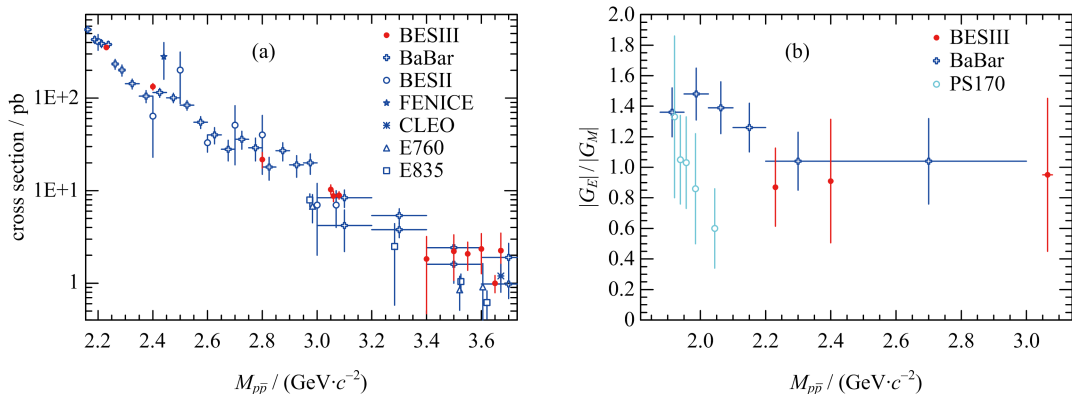
The proton FFs have also been measured with the large XYZ dataset collected at BESIII by means

of ISR technique, which allows a continuous  $q^2$  measurement from the threshold. Detection efficiency depends slowly on  $q^2$  and it is about 20% with  $\gamma_{\text{ISR}}$ -untagged mode, and about 6% with  $\gamma_{\text{ISR}}$ -tagged mode. Full angular distribution in hadronic center-of-mass is acquired, and the acceptance at threshold is non-zero, in the untagged mode. BESIII statistics is competitive with BABAR above  $M(p\bar{p}) \sim 2.0$  GeV.

## 2 Neutron FFs

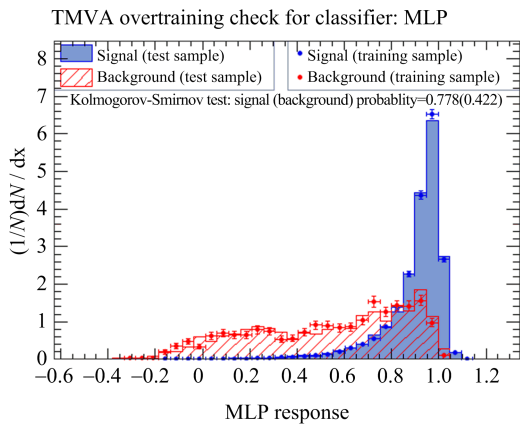
Up to now, the experimental results on neutron FFs are very few. Only FENICE<sup>[5]</sup> and SND<sup>[17]</sup> gave results about neutron effective FFs. This is due to the difficulties in detecting low energy  $n$ , when the  $n$  does not produce a hadronic shower yet in the electromagnetic calorimeter (EMC). The  $\bar{n}$  always annihilates and releases a large amount of hadronic energy, more than twice the nucleon mass. The sources of background in detecting an  $\bar{n}$  are other neutral particles, like  $\gamma$ ,  $K_L^0$  and mostly beam and neutral cosmic rays.

At BESIII, the depth of the EMC is about 15 electromagnetic radiation lengths, and about 50% of a hadronic interaction length, which is roughly the probability of detecting high energy  $n$  and  $\bar{n}$  interacting in the EMC. For a 1 GeV photon the EMC energy resolution is 2.5% in the barrel and 5.0% in the end-caps, which provides a chance to reconstruct at least the  $\bar{n}$ . The measurements can be performed by means of  $e^+e^- \rightarrow n\bar{m}$  with the



**Fig. 1 The Born cross section (a) and  $R$  (b) from BESIII compared with other measurements**

scanned data and by means of the radiative return  $e^+e^- \rightarrow \gamma_{\text{ISR}} \bar{n}m$  using the XYZ data. The detection strategy could be: first identify  $\bar{n}$  and  $\gamma_{\text{ISR}}$ ; then the EMC shower information is used in those cases where  $n$  identification is possible; finally event kinematics is used to further veto the remaining background. The EMC capability in distinguishing between  $\bar{n}$  and photon is comprehensively studied with the Toolkit for Multivariate Data Analysis in the ROOT (TMVA) package. The result is shown in Fig. 2, where one can see that  $\bar{n}$  and photon are well separated.



The hatched histogram and dots represent signal.

The other histogram and dots are for background from a photon.

**Fig. 2** The EMC capability in distinguishing between  $\bar{n}$  and photon studied with TMVA package

To increase the overall detection efficiency, relaxing  $n$  identification, the muon counter (MUC) and the TOF counters can be exploited. MUC is made of Resistive Plate Counters interleaved with the yoke iron. The yoke iron is about  $54 \sim \text{cm}$  in total, which makes  $\sim 96\%$  the probability the  $\bar{n}$  interacts in MUC. TOF counters are fired by the  $\bar{n}$  annihilation star and the TOF measurement might be enough to get rid of  $n$  detection. So these are additional possibilities to detect  $\bar{n}$  at BESIII, and their feasibility is under study.

### 3 $\Lambda$ FFs

The Coulomb factor should not enter the cross section formula in the case of a neutral baryon pair. Therefore the Born cross section is expected

to vanish at threshold, increasing with the velocity of the baryon. The  $\Lambda\bar{\Lambda}$  cross section and FFs have been measured by BABAR by means of ISR technique, from threshold to  $2.27 \text{ GeV}$ , with a non-zero cross section of  $(204 \pm 60 \pm 20) \text{ pb}$  at threshold. This result may conflict with the theory prediction but it is integrated on a large energy interval, because of ISR.

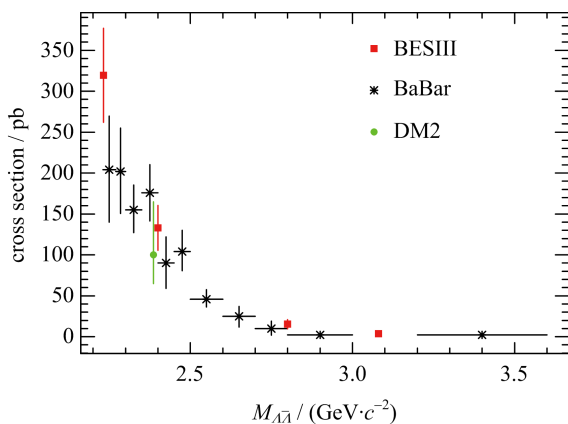
With the data collected in 2012, the FFs of  $\Lambda\bar{\Lambda}$  have been measured at BESIII preliminarily at four energy points,  $2232.4, 2400.0, 2800.0, 3080.0 \text{ MeV}$  and a search has been done by looking at  $\Lambda \rightarrow p\pi^-$  and  $\Lambda \rightarrow n\pi^0$ . At  $2232.4 \text{ MeV}$ , very close to the threshold, the momentum of the final proton is too low to leave a message in the detector and the antiproton interacts on the beam pipe. However it is possible to exploit the fact that in the  $\Lambda \rightarrow \bar{p}\pi^0$  decaying vertex of the secondary particles produced by  $\bar{p}$  in the beam pipe is  $3 \sim \text{cm}$  displaced, due to the interaction with the beam pipe. For  $\Lambda \rightarrow n\pi^0$  selection, the TMVA based on Boosted Decision Tree is applied to veto large background. The  $\pi^0$  in the final state has a monochromatic momentum, about  $105 \text{ MeV}$ . According to the aforementioned features,  $43 \pm 7$  events have been selected from  $\Lambda \rightarrow \bar{p}\pi^0$  mode, and  $22 \pm 6$  events from  $\Lambda \rightarrow n\pi^0$  mode. Surprisingly, a large cross section, about  $(320 \pm 58) \text{ pb}$  very close ( $\sim 1 \text{ MeV}$  above) to the threshold has been observed. Cross section and effective FF are listed in Table. 2. Fig. 3 shows  $\Lambda\bar{\Lambda}$  cross section, as measured by BESIII, BABAR<sup>[18]</sup> and DM2<sup>[4]</sup>.

Due to parity violating decay of  $\Lambda \rightarrow p\pi$ , the proton emission depends on  $\Lambda$  polarization in the  $\Lambda\bar{\Lambda}$  frame. The imaginary part of FFs leads to a polarization observable, as shown in Eq. (6).  $\theta_\Lambda$  is the polar angle of  $\Lambda$  in  $\Lambda\bar{\Lambda}$  frame.  $\theta_p$  is the polar angle of  $p$  in  $\Lambda$  frame. According to the data taken in 2014 and 2015, a statistical accuracy between  $6\%$  and  $17\%$  for  $P_n$  can be achieved.

$$P_n = -\frac{\sin 2\theta \sin \Delta\phi / \tau}{R \sin^2 \theta_\Lambda \tau + (1 + \cos^2 \theta_\Lambda) / R} = \frac{3}{\alpha_\Lambda} \langle \cos \theta_p \rangle \quad (6)$$

**Tab. 2 BESIII results on  $\Lambda\bar{\Lambda}$  cross section and effective form factor**

$\sqrt{s}/\text{MeV}$	$\sigma_{\text{Born}}/\text{pb}$	$ G (\times 10^{-2})$
2 232. 4		
$\Lambda \rightarrow p\pi^-, \bar{\Lambda} \rightarrow \bar{p}\pi^+$	$325 \pm 53 \pm 46$	
$\bar{\Lambda} \rightarrow \bar{n}\pi^0$	$(3.0 \pm 1.0 \pm 0.4) \times 10^2$	
combined	$320 \pm 58$	$63.4 \pm 5.7$
2 400. 0	$133 \pm 20 \pm 19$	$12.93 \pm 0.97 \pm 0.92$
2 800. 0	$15.3 \pm 5.4 \pm 2.0$	$4.16 \pm 0.73 \pm 0.27$
3 080. 0	$3.9 \pm 1.1 \pm 0.5$	$2.21 \pm 0.31 \pm 0.14$



**Fig. 3 BESIII, BABAR and DM2 measurements of  $\Lambda\bar{\Lambda}$  from 2. 0 up to 3. 6 GeV**

## 4 FFs of $\Lambda_c$ and other hyperons

The Coulomb enhancement factor  $\mathcal{C}$  at threshold, in the case of  $e^+e^- \rightarrow \Lambda_c \bar{\Lambda}_c$  predicts  $\sigma_{\text{Born}} = \frac{\pi^2 \alpha^3}{2M^2} |G|^2 = 0.15 |G|^2$  nb. Results from Belle<sup>[19]</sup> indicate that the cross section near the threshold of  $\Lambda_c \bar{\Lambda}_c$  is nearly 0.15 nb, which means  $G \sim 1$  at threshold. This strange result is consistent with what has been found by BABAR in  $e^+e^- \rightarrow p\bar{p}$ . Also the ratio  $R$ , as measured by BABAR, might be unexpected, being different from 1 (but integrated on an energy interval) as expected according to analyticity. However, the Belle result is affected by a very large uncertainty. To verify this, more integrated luminosity is needed. BESIII collected at 4575  $\sim$  MeV, very close to the threshold, an integrated luminosity of 42 pb<sup>-1</sup>. Very likely, BESIII will collect more data at high energy. Thus, the cross section

measurement will be largely improved, and a 10% precision in the measurement of  $R$  is expected with a luminosity of 200 pb<sup>-1</sup>, assuming an  $R$  value similar to the one found in the proton case at BABAR.

Taking the advantage of the large energy range and large data samples at BESIII, the TL-FFs of other hyperons, such as  $\Lambda \bar{\Sigma}^0$ ,  $\bar{\Sigma}^0 \Sigma^0$ ,  $\bar{\Sigma}^- \Sigma^+$ ,  $\bar{\Sigma}^+ \Sigma^-$ ,  $\bar{\Xi}^0 \Xi^0$ ,  $\bar{\Xi}^+ \Xi^-$ ,  $\bar{\Omega}^+ \Omega^-$ , together with the measurements of  $R$  and relative phase  $\Delta\Phi$  at single energy points will be extracted.

## 5 Conclusion

BESIII is an excellent laboratory for baryon form factor measurements. Both scan and ISR techniques can be used. The proton FFs and the ratio have been measured using 2011~2013 data. With the same data, preliminary results on  $\Lambda\bar{\Lambda}$  have been just released. With higher statistics between 2.0 and 3.1 GeV, collected in 2014 and 2015, new significant results will come and improve FFs status for  $p$ ,  $n$ ,  $\Lambda$ ,  $\Xi$ ,  $\Omega$ ,  $\Sigma$ ,  $\Lambda_c$ . Also the measurements with XYZ datasets by ISR method are worth anticipating.

## References

- [1] HALZEN F, MARTIN A D. Quarks and Leptons: An Introductory Course in Modern Particle Physics[M]. Canada: John Wiley&Sons,1984;172.
- [2] DELCOURT B, DERADO I, BERTRAND J L, et al. Study of the reaction  $e^+e^- \rightarrow p\bar{p}$  in the total energy range 1925 - 2180 MeV [J]. Phys Lett B, 1982, 86(3/4): 395-398.
- [3] BISELLO D, LIMENTANI S, NIGRO M, et al. A measurement of  $e^+e^- \rightarrow p\bar{p}$  for  $(1975 \leq \sqrt{s} \leq 2250)$  MeV[J]. Nucl Phys B,1983, 224(3):379-395.
- [4] BISELLO D, BUSETTO G, CASTRO A, et al. Baryon pairs production in  $e^+e^-$  annihilation at  $\sqrt{s}=2.4$  GeV[J]. Z Phys C,1990, 48(1): 23-28.
- [5] ANTONELLI A, BALDINI R, BENASI P, et al. The first measurement of the neutron electromagnetic form factors in the time-like region[J]. Nucl Phys B,1998, 517(1/2/3):3-35.
- [6] ABLIKIM M, BAI J Z, BAN Y, et al. Measurement of the cross section for image at center-of-mass energies

- from 2.0 to 3.07 GeV [J]. Phys Lett B, 2005, 630(1/2): 14-20.
- [7] PEDLAR TK, CRONIN-HENNESSY D, GAO K Y, et al. Precision measurements of the timelike electromagnetic form factors of pion, kaon, and proton [J]. Phys Rev Lett, 2005, 95:261803.
- [8] AUBERT B, BARATE R, BOUTIGNY D, et al. Study of  $e^+e^- \rightarrow p\bar{p}$  using initial state radiation with BABAR [J]. Phys Rev D, 2006, 73:012005.
- [9] LEES J P, POIREAU V, TISSERAND V, et al. Study of  $e^+e^- \rightarrow p\bar{p}$  via initial-state radiation at BABAR [J]. Phys Rev D, 2013, 87:092005.
- [10] LEES J P, POIREAU V, TISSERAND V, et al. Measurement of the  $e^+e^- \rightarrow p\bar{p}$  cross section in the energy range from 3.0 to 6.5 GeV [J]. Phys Rev D, 2013, 88:072009.
- [11] BARDIN G, BURGUN G, CALABRESE R, et al. Determination of the electric and magnetic form factors of the proton in the time-like region [J]. Nucl Phys B, 1994, 411(1):3-32.
- [12] ARMSTRONG T A, BETTONI D, BHARADWAJ V, et al. Proton electromagnetic form factors in the timelike region from 8.9 to 13.0 GeV<sup>2</sup> [J]. Phys Rev Lett, 1993, 70:1 212.
- [13] AMBROGIANI M, BAGNASCO S, BALDINI W, et al. Measurements of the magnetic form factor of the proton in the timelike region at large momentum transfer [J]. Phys Rev D, 1999, 60:032002.
- [14] ANDREOTTI M, BAGNASCO S, BALDINI W, et al. Measurements of the magnetic form factor of the proton for timelike momentum transfers [J]. Phys Lett B, 2003, 559(1/2):20-25.
- [15] ABLIKIM M, ACHASOV M N, AI X C, et al. Measurement of the proton form factor by studying  $e^+e^- \rightarrow p\bar{p}$  [J]. Phys Rev D, 2015, 91:112004.
- [16] Ping R G. An exclusive event generator for  $e^+e^-$  scan experiments [J]. Chin Phys C, 2014, 38(8):083001.
- [17] ACHASOV M N, BARNYAKOV A YU, BELOBORODOV K I, et al. Study of the process  $e^+e^- \rightarrow m\bar{m}$  at the VEPP-2000  $e^+e^-$  collider with the SND detector [J]. Phys Rev D, 2014, 90: 112007.
- [18] AUBERT B, BONA M, BOUTIGNY D, et al. Study of  $e^+e^- \rightarrow \Lambda\bar{\Lambda}, \Lambda\bar{\Sigma}^0, \Sigma^0\bar{\Sigma}^0$  using initial state radiation with BABAR [J]. Phys Rev D, 2007, 76:092006.
- [19] PAKHLOVA G, ADACHI I, AIHARA H, et al. Observation of a near-threshold enhancement in the  $e^+e^- \rightarrow \Lambda_c^+\Lambda_c^-$  cross section using initial-state radiation [J]. Phys Rev Lett, 2008, 101:172001.